Economics 101A (Lecture 18)

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Outline

- 1. Supply Function
- 2. One-step Profit Maximization
- 3. Introduction to Market Equilibrium
- 4. Aggregation
- 5. Market Equilibrium in the Short-Run

1 Supply Function

- Supply function: $y^* = y^* (w, r, p)$
- What happens to y^* as p increases?
- Is the supply function upward sloping?
- Remember f.o.c:

$$p - c_y'(w, r, y) = 0$$

• Implicit function:

$$\frac{\partial y^*}{\partial p} = -\frac{1}{-c_{y,y}''(w,r,y)} > 0$$

as long as s.o.c. is satisfied.

• Yes! Supply function is upward sloping.

2 One-step Profit Maximization

- Nicholson, Ch. 9, pp. 265–270 [OLD: Ch. 13, pp. 346–350].
- One-step procedure: maximize profits

- ullet Perfect competition. Price p is given
 - Firms are small relative to market
 - Firms do not affect market price p_M

- Will firm produce at $p > p_M$?
- Will firm produce at $p < p_M$?
- $\Longrightarrow p = p_M$

• Revenue: py = pf(L, K)

• Cost: wL + rK

• Profit pf(L,K) - wL - rK

Agent optimization:

$$\max_{L,K} pf(L,K) - wL - rK$$

First order conditions:

$$pf'_L(L,K) - w = 0$$

and

$$pf_K'(L,K) - r = 0$$

• Second order conditions? $pf_{L,L}''(L,K) < 0$ and

$$|H| = \begin{vmatrix} pf''_{L,L}(L,K) & pf''_{L,K}(L,K) \\ pf''_{L,K}(L,K) & pf''_{K,K}(L,K) \end{vmatrix} =$$

$$= p^2 \left[f''_{L,L}f''_{K,K} - \left(f''_{L,K} \right)^2 \right] > 0$$

ullet Need $f_{L.K}^{\prime\prime}$ not too large for maximum

- ullet Comparative statics with respect to to p, w, and r.
- What happens if w increases?

$$\frac{\partial L^{*}}{\partial w} = -\frac{\begin{vmatrix} -1 & pf''_{L,K}(L,K) \\ 0 & pf''_{K,K}(L,K) \end{vmatrix}}{\begin{vmatrix} pf''_{L,L}(L,K) & pf''_{L,K}(L,K) \\ pf''_{L,K}(L,K) & pf''_{K,K}(L,K) \end{vmatrix}} < 0$$

and

$$\frac{\partial L^*}{\partial r} =$$

• Sign of $\partial L^*/\partial r$ depends on $f_{L,K}''$.

3 Introduction to Market Equilibrium

- Nicholson, Ch. 10, pp. 279–295 [OLD: Ch. 14, pp. 368–382.
- Two ways to analyze firm behavior:
 - Two-Step Cost Minimization
 - One-Step Profit Maximization

- What did we learn?
 - Optimal demand for inputs L^* , K^* (see above)
 - Optimal quantity produced y^*

- Supply function. $y = y^*(p, w, r)$
 - From profit maximization:

$$y = f(L^*(p, w, r), K^*(p, w, r))$$

- From cost minimization:

$$MC$$
 curve above AC

- Supply function is increasing in p

• Market Equilibrium. Equate demand and supply.

- Aggregation?
- Industry supply function!

4 Aggregation

4.1 Producers aggregation

- ullet J companies, j=1,...,J, producing good i
- Company j has supply function

$$y_i^j = y_i^{j*}(p_i, w, r)$$

• Industry supply function:

$$Y_i(p_i, w, r) = \sum_{j=1}^{J} y_i^{j*}(p_i, w, r)$$

• Graphically,

4.2 Consumer aggregation

- Nicholson, Ch. 10, pp. 279–282 [OLD: Ch. 7, pp. 172–176]
- One-consumer economy
- Utility function $u(x_1, ..., x_n)$
- prices $p_1, ..., p_n$
- Maximization ⇒

$$x_1^* = x_1^* (p_1, ..., p_n, M),$$

 \vdots
 $x_n^* = x_n^* (p_1, ..., p_n, M).$

ullet Focus on good i. Fix prices $p_1,...,p_{i-1},p_{i+1},...,p_n$ and M

• Single-consumer demand function:

$$x_i^* = x_i^* (p_i|p_1, ..., p_{i-1}, p_{i+1}, ..., p_n, M)$$

- What is sign of $\partial x_i^*/\partial p_i$?
- Negative if good i is normal
- Negative or positive if good i is inferior

- ullet Aggregation: J consumers, j=1,...,J
- ullet Demand for good i by consumer j:

$$x_i^{j*} = x_i^{j*} (p_1, ..., p_n, M^j)$$

• Market demand X_i :

$$X_{i} \left(p_{1}, ..., p_{n}, M^{1}, ..., M^{J} \right)$$

$$= \sum_{j=1}^{J} x_{i}^{j*} \left(p_{1}, ..., p_{n}, M^{j} \right)$$

• Graphically,

 \bullet Notice: market demand function depends on distribution of income ${\cal M}^J$

- Market demand function X_i :
 - Consumption of good i as function of prices ${f p}$
 - Consumption of good i as function of income distribution ${\cal M}^j$

5 Market Equilibrium in the Short-Run

- Nicholson, Ch. 14, pp. 368–382.
- What is equilibrium price p_i ?
- Magic of the Market...
- Equilibrium: No excess supply, No excess demand
- Prices p^* equates demand and supply of good i:

$$Y^* = Y_i^S(p_i^*, w, r) = X_i^D(p_1^*, ..., p_n^*, M^1, ..., M^J)$$

•	Graphic	cally,					
•	Notice:	in short-rı	un firm	s can	make	positive	profits

•	Comparative statics	exercises	with	endogenous	price
	p_i :				

- increase in wage w or interest rate r:

- change in income distribution

6 Comparative statics of equilibrium

ullet Supply and Demand function of parameter lpha :

$$-Y_{i}^{S}\left(p_{i},w,r,\alpha\right)$$

$$-X_{i}^{D}(\mathbf{p}, \mathbf{M}, \alpha)$$

- How does α affect p^* and Y^* ?
- ullet Comparative statics with respect to lpha

• Equilibrium:

$$Y_i^S(p_i, w, r, \alpha) = X_i^D(\mathbf{p}, \mathbf{M}, \alpha)$$

• Can write equilibrium as implicit function:

$$Y_i^S(p_i, w, r, \alpha) - X_i^D(\mathbf{p}, \mathbf{M}, \alpha) = \mathbf{0}$$

- What is $dp^*/d\alpha$?
- Implicit function theorem:

$$\frac{\partial p^*}{\partial \alpha} = -\frac{\frac{\partial Y^S}{\partial \alpha} - \frac{\partial X^D}{\partial \alpha}}{\frac{\partial Y^S}{\partial p} - \frac{\partial X^D}{\partial p}}$$

• What is sign of denominator?

ullet Sign of $\partial p^*/\partial lpha$ is negative of sign of numerator

• Examples:

1. Fad. Good becomes more fashionable: $\frac{\partial X^D}{\partial \alpha} > 0 \Longrightarrow \frac{\partial p^*}{\partial \alpha} > 0$

- 2. Recession in Europe. Negative demand shock for US firms: $\frac{\partial X^D}{\partial \alpha} < 0 \Longrightarrow \frac{\partial p^*}{\partial \alpha} < 0$
- 3. Oil shock. Import prices increase: $\frac{\partial Y^S}{\partial \alpha} < 0 \Longrightarrow \frac{\partial p^*}{\partial \alpha} > 0$

4. Computerization. Improvement in technology. $\frac{\partial Y^S}{\partial \alpha} > 0 \Longrightarrow \frac{\partial p^*}{\partial \alpha} < 0$

7 Next Lecture

- Elasticities
- Taxes and Subsidies
- Long-Run Equilibrium