Economics 101A (Lecture 18)

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Outline

- 1. Comparative Statics of Equilibrium
- 2. Elasticities
- 3. Response to Taxes
- 4. Trade

1 Comparative statics of equilibrium

- Nicholson, Ch. 12, pp. 403-406 (Ch. 10, pp. 293-295, 9th)
- Supply and Demand function of parameter α :

-
$$Y_i^S(p_i, w, r, \alpha)$$

-
$$X_i^D(\mathbf{p}, \mathbf{M}, \alpha)$$

- How does α affect p^* and Y^* ?
- $\bullet\,$ Comparative statics with respect to $\alpha\,$

• Equilibrium:

$$Y_i^S(p_i, w, r, \alpha) = X_i^D(\mathbf{p}, \mathbf{M}, \alpha)$$

• Can write equilibrium as implicit function:

$$Y_i^S(p_i, w, r, \alpha) - X_i^D(\mathbf{p}, \mathbf{M}, \alpha) = \mathbf{0}$$

- What is $dp^*/d\alpha$?
- Implicit function theorem:

$$\frac{\partial p^*}{\partial \alpha} = -\frac{\frac{\partial Y^S}{\partial \alpha} - \frac{\partial X^D}{\partial \alpha}}{\frac{\partial Y^S}{\partial p} - \frac{\partial X^D}{\partial p}}$$

• What is sign of denominator?

• Sign of $\partial p^*/\partial \alpha$ is negative of sign of numerator

- Examples:
 - 1. *Fad.* Good becomes more fashionable: $\frac{\partial X^D}{\partial \alpha} > 0 \implies \frac{\partial p^*}{\partial \alpha} > 0$
 - 2. Recession in Europe. Negative demand shock for US firms: $\frac{\partial X^D}{\partial \alpha} < 0 \Longrightarrow \frac{\partial p^*}{\partial \alpha} < 0$
 - 3. *Oil shock.* Import prices increase: $\frac{\partial Y^S}{\partial \alpha} < 0 \implies \frac{\partial p^*}{\partial \alpha} > 0$
 - 4. Computerization. Improvement in technology. $\frac{\partial Y^S}{\partial \alpha} > 0 \Longrightarrow \frac{\partial p^*}{\partial \alpha} < 0$

2 Elasticities

- Nicholson, Ch.1, pp. 26-27 (pp. 27-28, 9th)
- How do we interpret magnitudes of $\partial p^* / \partial \alpha$?
- Result depends on units of measure.
- Can we write $\partial p^* / \partial \alpha$ in a unit-free way?
- Yes! Use elasticities.
- Elasticity of x with respect to parameter p is

$$\varepsilon_{x,p} = \frac{\partial x \, p}{\partial p \, x}$$

• Interpretation: Percent response in x to percent change in p :

$$\varepsilon_{x,p} = \frac{\partial x p}{\partial p x} = \lim_{dp \to 0} \frac{x (p + dp) - x (p) p}{dp x} = \lim_{dp \to 0} \frac{dx/x}{dp/p}$$

where $dx \equiv x (p + dp) - x (p)$.

• Now, show

$$\varepsilon_{x,p} = \frac{\partial \ln x}{\partial \ln p}$$

• Notice: This makes sense only for x > 0 and p > 0

• Proof. Consider function

$$x = f(p)$$

• Rewrite as

$$\ln(x) = \ln f(p) = \ln f\left(e^{\ln(p)}\right)$$

- Define $\hat{x} = \ln(x)$ and $\hat{p} = \ln(p)$
- This implies

$$\hat{x} = \ln f\left(e^{\hat{p}}\right)$$

• Get

$$\begin{aligned} \frac{\partial \hat{x}}{\partial \hat{p}} &= \frac{\partial \ln x}{\partial \ln p} = \\ &= \frac{1}{f\left(e^{\hat{p}}\right)} \frac{\partial f\left(e^{\hat{p}}\right)}{\partial \hat{p}} e^{\hat{p}} = \frac{\partial x p}{\partial p x} \end{aligned}$$

• Example with Cobb-Douglas utility function

•
$$U(x,y) = x^{\alpha}y^{1-\alpha}$$
 implies solutions

$$x^* = \alpha \frac{M}{p_x}, y^* = (1 - \alpha) \frac{M}{p_y}$$

• Elasticity of demand with respect to own price ε_{x,p_x} :

$$\varepsilon_{x,p_x} = \frac{\partial x^*}{\partial p_x} \frac{p_x}{x^*} = -\frac{\alpha M}{(p_x)^2} \frac{p_x}{\alpha \frac{M}{p_x}} = -1$$

• Elasticity of demand with respect to other price $\varepsilon_{x,p_y} = 0$

• Go back to problem above:

$$\frac{\partial p^*}{\partial \alpha} = -\frac{\frac{\partial Y^S}{\partial \alpha} - \frac{\partial X^D}{\partial \alpha}}{\frac{\partial Y^S}{\partial p} - \frac{\partial X^D}{\partial p}}$$

• Use elasticities to rewrite response of p to change in α :

$$\frac{\partial p^* \alpha}{\partial \alpha p} = -\frac{\left(\frac{\partial Y^S}{\partial \alpha} - \frac{\partial X^D}{\partial \alpha}\right) \frac{\alpha}{Y}}{\left(\frac{\partial Y^S}{\partial p} - \frac{\partial X^D}{\partial p}\right) \frac{p}{Y}}$$

or (using fact that $X^{D*} = Y^{s*}$)

$$\varepsilon_{p,\alpha} = -\frac{\varepsilon_{S,\alpha} - \varepsilon_{D,\alpha}}{\varepsilon_{S,p} - \varepsilon_{D,p}}$$

• We are likely to know elasticities from empirical studies

3 Response to taxes

- Nicholson, Ch. 12, pp. 423-426 (Ch. 11, pp. 322– 323, 9th)
- Per-unit tax t
- Write price p_i as price including tax
- Supply: $Y_i^S(p_i t, w, r)$
- Demand: $X_i^D(\mathbf{p}, \mathbf{M})$ $Y_i^S(p_i - t, w, r) - X_i^D(\mathbf{p}, \mathbf{M}) = 0$
- What is dp^*/dt ?

• Comparative statics:

$$\begin{aligned} \frac{\partial p^*}{\partial t} &= -\frac{\frac{\partial Y^S}{\partial t}}{\frac{\partial Y^S}{\partial p} - \frac{\partial X^D}{\partial p}} = \\ &= -\frac{-\frac{\frac{\partial Y^S}{\partial p} \frac{p}{X}}{\frac{\partial Y^S}{\partial p} - \frac{\partial X^D}{\partial p}} = \\ &= \frac{\varepsilon_{S,p}}{\varepsilon_{S,p} - \varepsilon_{D,p}} \end{aligned}$$

• How about price received by suppliers $p^* - t$?

$$\frac{\partial (p^* - t)}{\partial t} = \frac{\frac{\partial Y^S}{\partial p}}{\frac{\partial Y^S}{\partial p} - \frac{\partial X^D}{\partial p}} - 1 = \frac{\varepsilon_{D,p}}{\varepsilon_{S,p} - \varepsilon_{D,p}}$$

• Inflexible Supply. (Capacity is fixed) Supply curve vertical ($\varepsilon_{S,p} = 0$)

- Producers bear burden of tax
- Flexible Supply. (Constant Returns to Scale) Supply curve horizontal $(\varepsilon_{S,p} \to \infty)$

• Consumers bear burden of tax

• Inflexible demand. Demand curve vertical ($\varepsilon_{D,p} = 0$)?

- Consumers bear burden
- General lesson: Least elastic side bears larger part of burden
- What happens with a subsidy (t < 0)?
- What happens to quantity sold?
- Use demand curve:

$$\frac{\partial X^{D*}}{\partial t} = \frac{\partial X^{D*}}{\partial p^*} \frac{\partial p^*}{\partial t}$$

and use expression for $\partial p^* / \partial t$ above

4 Trade

- Nicholson, Ch. 12, pp. 427-429 (Ch. 11, pp. 326– 327, 9th)
- Assume that domestic industry opens to trade
- Is this a good or a bad thing?
- Consider graphically
- Equilibrium with no trade at quantity X_D^\ast and price p_D^\ast

- $\bullet\,$ Trade: Goods available at lower price p_T^*
- (Otherwise, opennness to trade irrelevant)

- Shift in price to $p_{T}^{\ast} < p_{D}^{\ast}$ and in quantity to $X_{T}^{\ast} > X_{D}^{\ast}$

• Label domestic production and imports

• What happens to profits of domestic firms?

• What happens to consumer suprlus?

 More total surplus, but firms lost some profits and some employment -> Difficult trade-off

• Define surplus formally in next lecture

5 Next Lecture

- Market Equilibrium in the Long-Run
- Consumer and Producer Surplus
- Market Power
- Monopoly
- Price Discrimination