

*Advanced Microeconomics*  
*(Economics 104)*  
*Fall 2007*  
*Problem Set III*  
*More on strategic games and maximization*

- Let  $G$  be a  $2 \times 2$  strategic game with game matrix

$$A = \begin{matrix} a_{11}, b_{11} & a_{12}, b_{12} \\ a_{21}, b_{21} & a_{22}, b_{22} \end{matrix},$$

and consider the game  $G'$  with game matrix  $A'$  which is derived from  $G$  by changing player 1's payoffs while keeping player 2's payoffs the same as they were in  $G$ . That is,

$$a_{ij} \neq a'_{ij} \text{ and } b_{ij} = b'_{ij}$$

for any  $i, j = 1, 2$ .

- Let  $p$  be a mixture over player 1's strategies and  $q$  be a mixture over player 2's strategies. Suppose that  $(p, q)$  is the unique equilibrium of  $G$  and  $(p', q')$  is the unique equilibrium of  $G'$ .

(i) Suppose that both equilibria are completely mixed. What can be said, if anything, about the relationship between  $(p, q)$  and  $(p', q')$ ?

(ii) Suppose that both equilibria are pure. What can be said, if anything, about the relationship between  $(p, q)$  and  $(p', q')$ ?

- Find player 1's max min and min max pure strategies in the following zero-sum game:  $A_1 = A_2 = [0, 1]$  and

$$u_1(a_1, a_2) = a_1 + 2a_2 - 4a_1a_2 + 1$$

where  $a_1 \in A_1$  and  $a_2 \in A_2$ .

- All other questions are from O chapter 11.

363.1 (max min in a bargaining game)

363.3 (Finding the max min)

364.2 ( $NE$  payoffs and max min payoffs)

365.1 ( $NE$  payoffs and max min payoffs)

366.2 (Determining strictly competitiveness)

369.2 ( $NE$  payoffs in symmetric game)

370.2 (max min in  $BoS$ )

372.1 (Increasing payoffs and eliminating actions)

372.2 ( $NE$  in strictly competitive game)